

# The Formation Histories of Galaxy Clusters

Santa Fe 05

M. White and JDC, astro-ph/0506213

...paper has extensive referencing, for  
talk it will be scarce.

As heard from Paul's talk this morning:

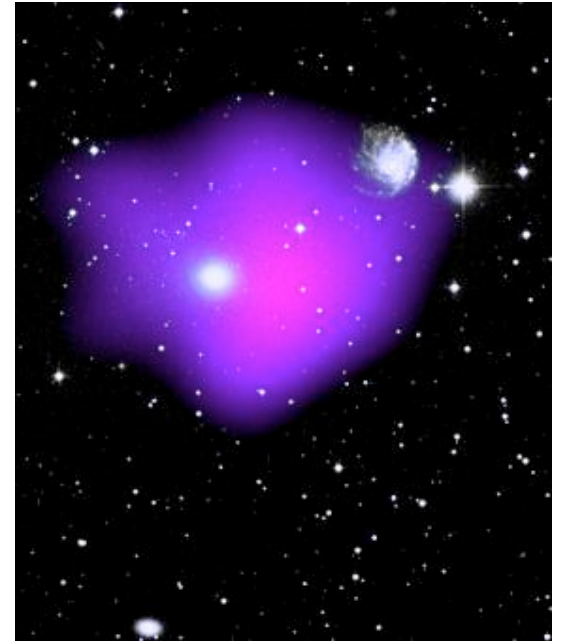
Galaxy clusters are the largest virialized systems  
in the universe.....

Number counts and clustering sensitive to  
cosmological parameters

Hosts of the largest known galaxies

Easy to count in dark matter simulations  
(big, so gas physics won't destroy)

Intensive studies of them underway for  
cosmology and intrinsic properties



NGC 2300  
ROSAT/STScI

Clusters are not only the **largest** collapsed objects.  
Hierarchical structure formation means they are also  
the **youngest**: many are still forming.

What does “still forming” mean?  
How do galaxy clusters form?

- Something you want to know for both cosmology and to learn about clusters themselves.
- Clusters are large and dark matter dominated
  - for large scale properties simulations can already tell us a lot: What do simulations give??

# Galaxy cluster formation

Simulate:

(starting from  $z=50$ )

gas  
density

galaxies  
(SAM)

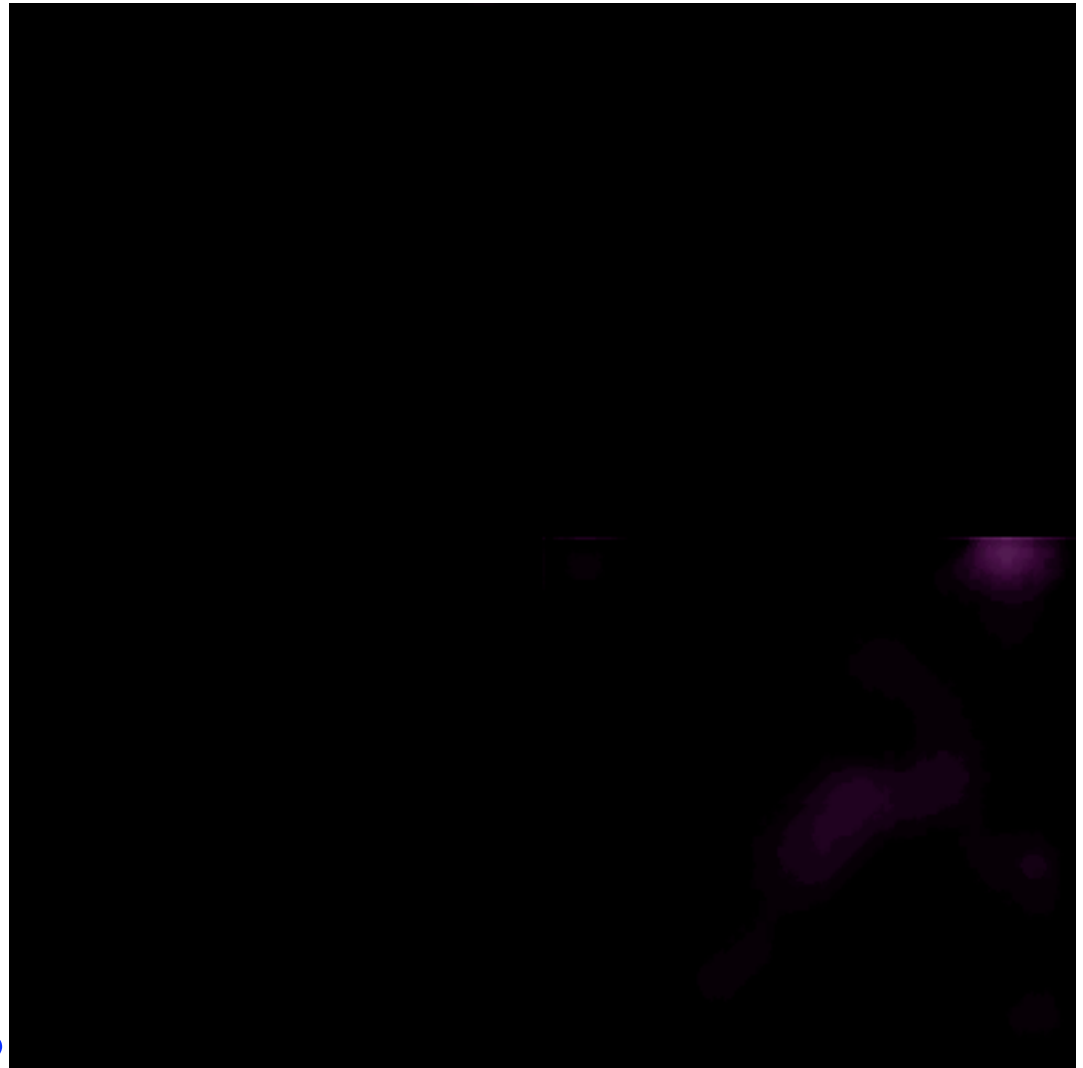
SZ

X-ray

$(10 h^{-1} \text{ Mpc})^3$  box

Complicated:

How to describe this???

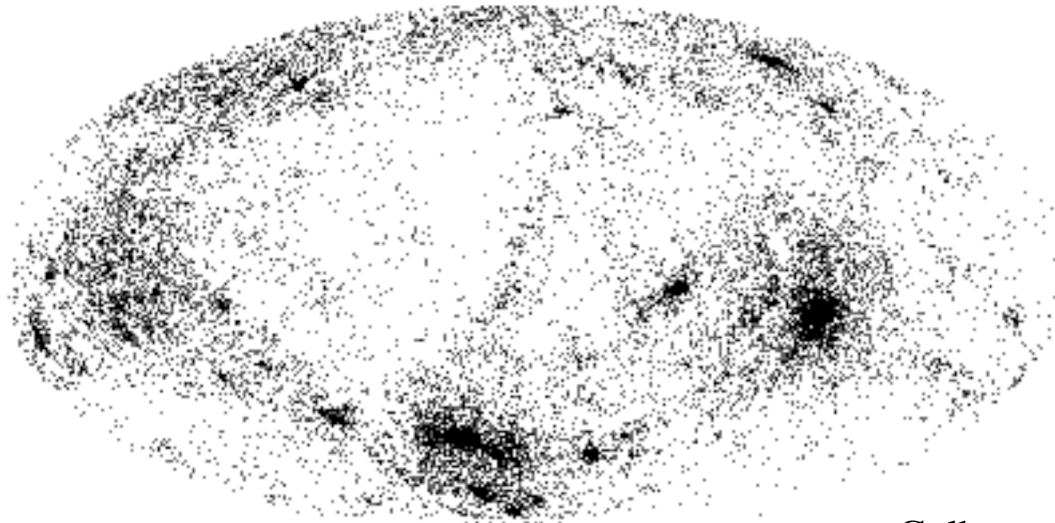


<http://astron.berkeley.edu/~mwhite/clusterform.mov>

Qualitatively: what is happening?

mergers and accretion:

hierarchical build up of clusters



Colberg et al, 1998

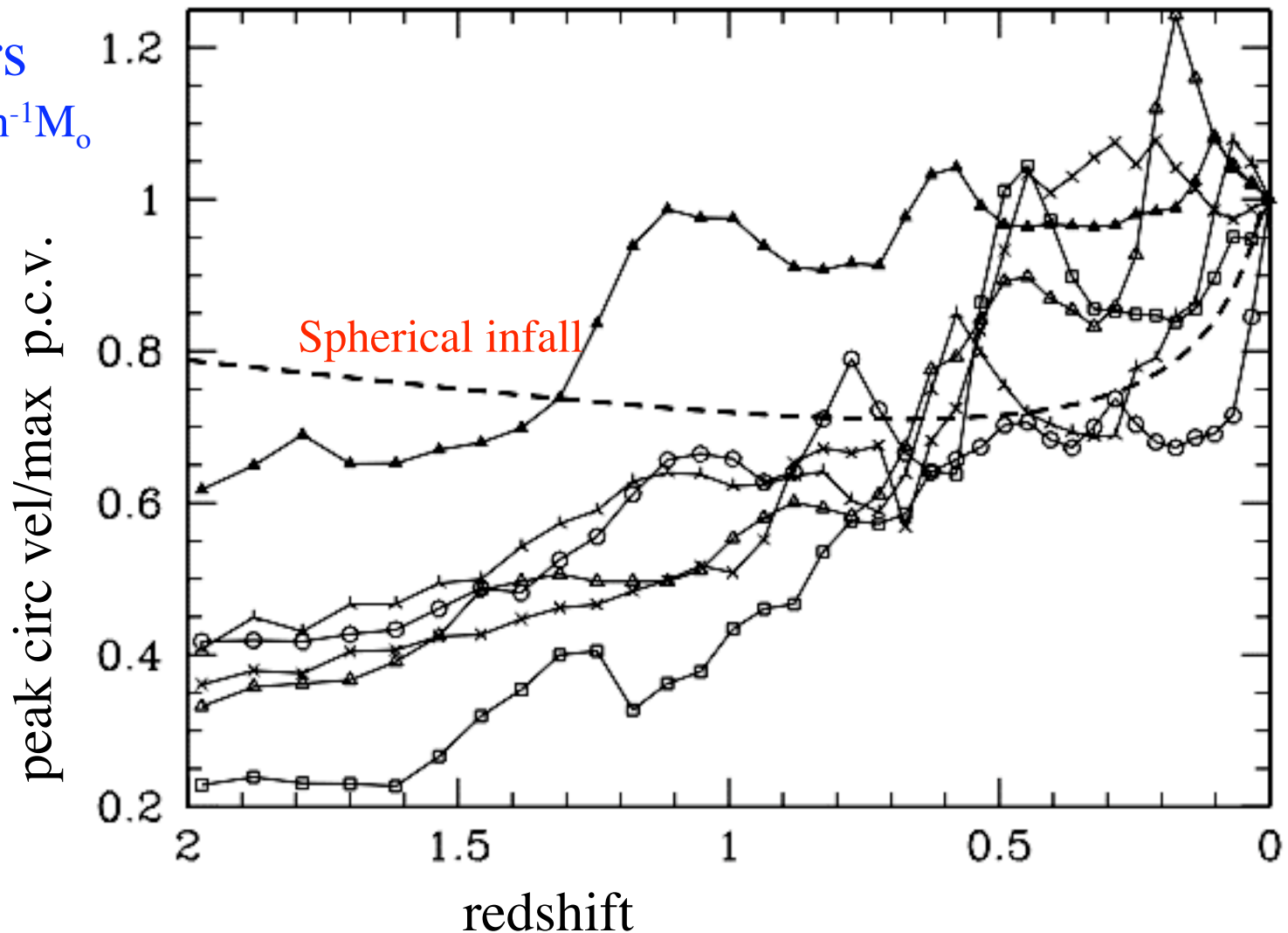
View from center of a cluster at  $z=0$

Process is lumpy/abrupt in space and time for any given cluster.

Also lots of scatter between different cluster histories:

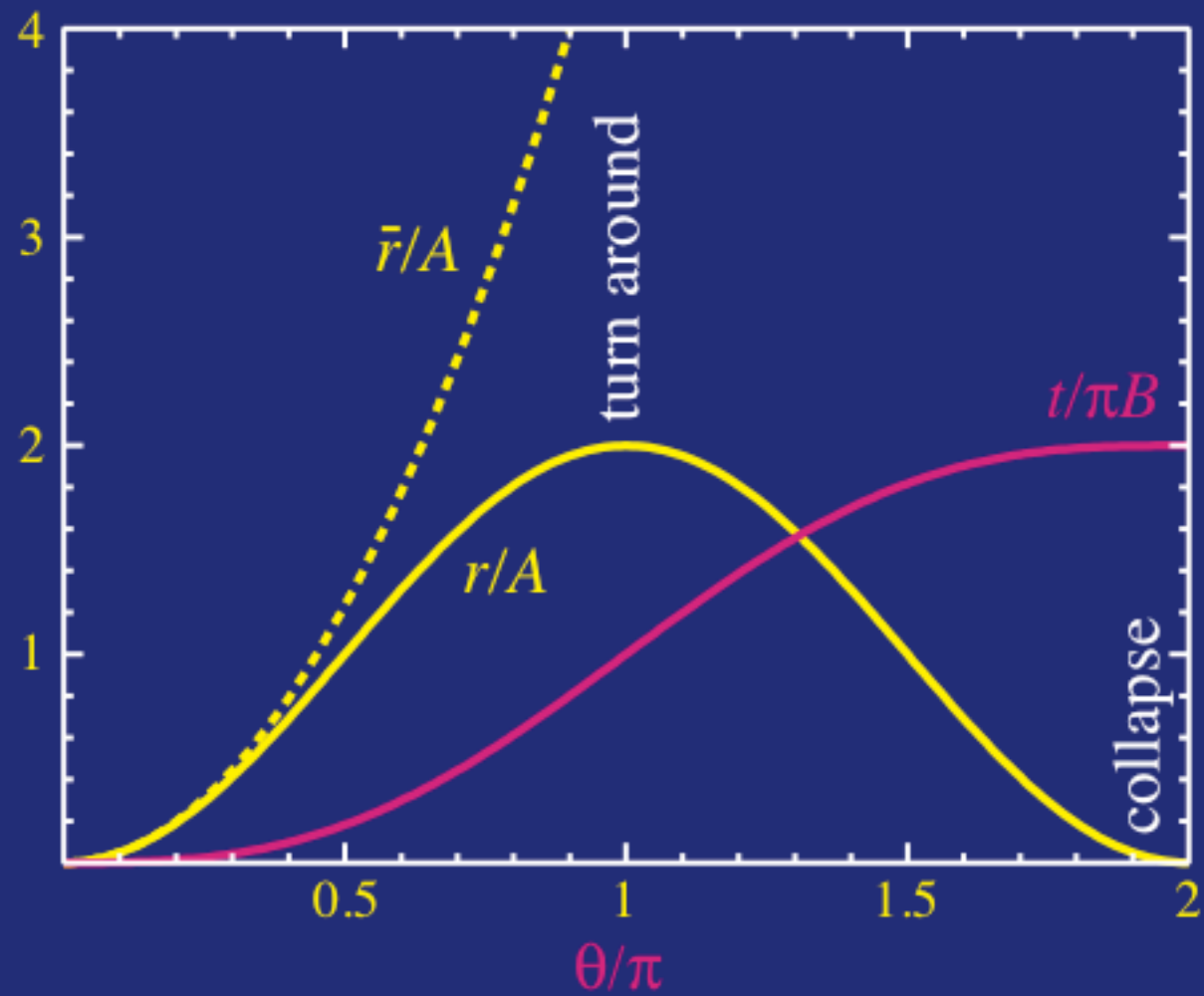
Six clusters

$M > 6 \times 10^{14} h^{-1} M_{\odot}$



(From N-body: rest of the results today will be from N-body as well)

- Parametric Solution:



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## CLOSED UNIVERSE

- A spherical perturbation of radius  $r$  behaves as a **closed universe**
- Radius  $r \propto a \rightarrow 0$ , collapse in finite time
- **Friedman equation** in a closed universe

$$\frac{1}{a} \frac{da}{dt} = H_0 \left( \Omega_m a^{-3} + (1 - \Omega_m) a^{-2} \right)^{1/2}$$

- Parametric solution in terms of a **development angle**  
 $\theta = H_0 \eta (\Omega_m - 1)^{1/2}$ , scaled conformal time  $\eta$

$$r(\theta) = A(1 - \cos \theta)$$

$$t(\theta) = B(\theta - \sin \theta)$$

where  $A = r_0 \Omega_m / 2(\Omega_m - 1)$ ,  $B = H_0^{-1} \Omega_m / 2(\Omega_m - 1)^{3/2}$ .

- Turn around at  $\theta = \pi$ ,  $r = 2A$ ,  $t = B\pi$ .
- Collapse at  $\theta = 2\pi$ ,  $r \rightarrow 0$ ,  $t = 2\pi B$

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# Characterize this cluster formation? (Quantitatively)

Many approaches in literature, e.g. using

- A single “formation time” (an event)
- A specific parameterization of the whole time history  $M(z)$
- Abrupt mass changes

Different definitions have different uses:

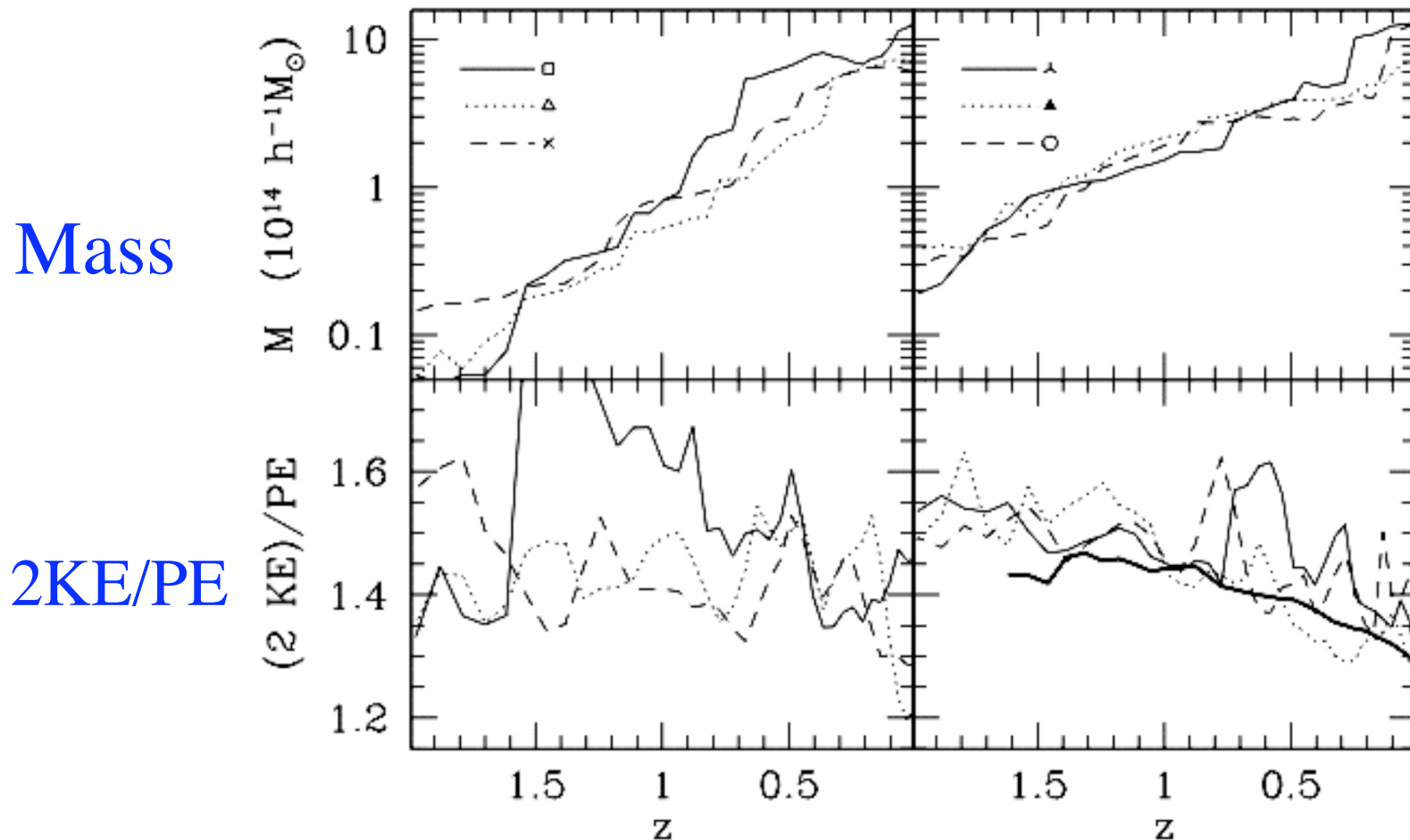
**when** a cluster formed depends on **why** you want to know!

Observables/selection functions depend upon formation process, and may guide which description is most appropriate. (more later)

# Characterize this cluster formation?

- A single “formation time” (an event)
- A specific parameterization of the whole time history  $M(z)$
- Abrupt mass changes

First try: when cluster has virialized, I.e. when  $2 \text{ KE} = \text{PE}$ :

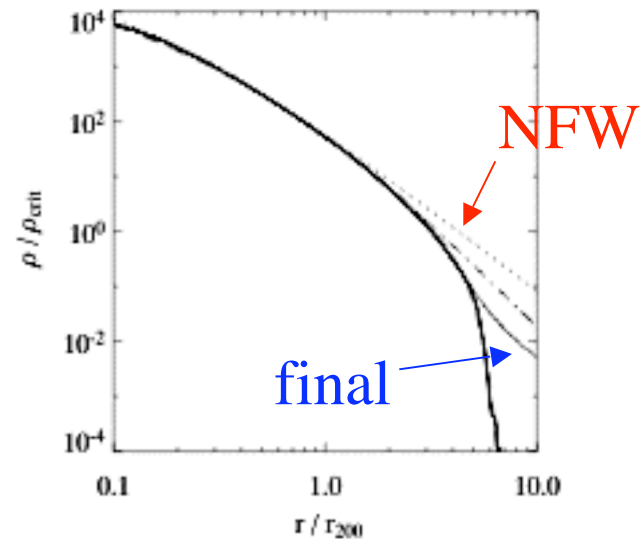


(heavy line: all clusters with  $M > 10^{14} h^{-1} M_{\odot}$  in  $(300 h^{-1} \text{ Mpc})^3$  box)

**No luck!!**      Constant infall of matter on cluster  
(...declines with decreasing  $z$  ( $z < 1$ ), decreasing mass)

Note: at very late times ( $a \gg 1$ ) there will not be infall on a cluster if  $\Lambda > 0$ :

clusters will be fully formed and relaxed  
lower density than NFW outside of  $r_{200}$   
(Nagamine & Loeb,  
Busha, Evrard, Adams, Wechsler)



But for now:

Because of infall: velocities are not easily related to simple equilibrium quantities.

Focus on something simpler:  $M(z)$ , cluster mass as fn of  $z$

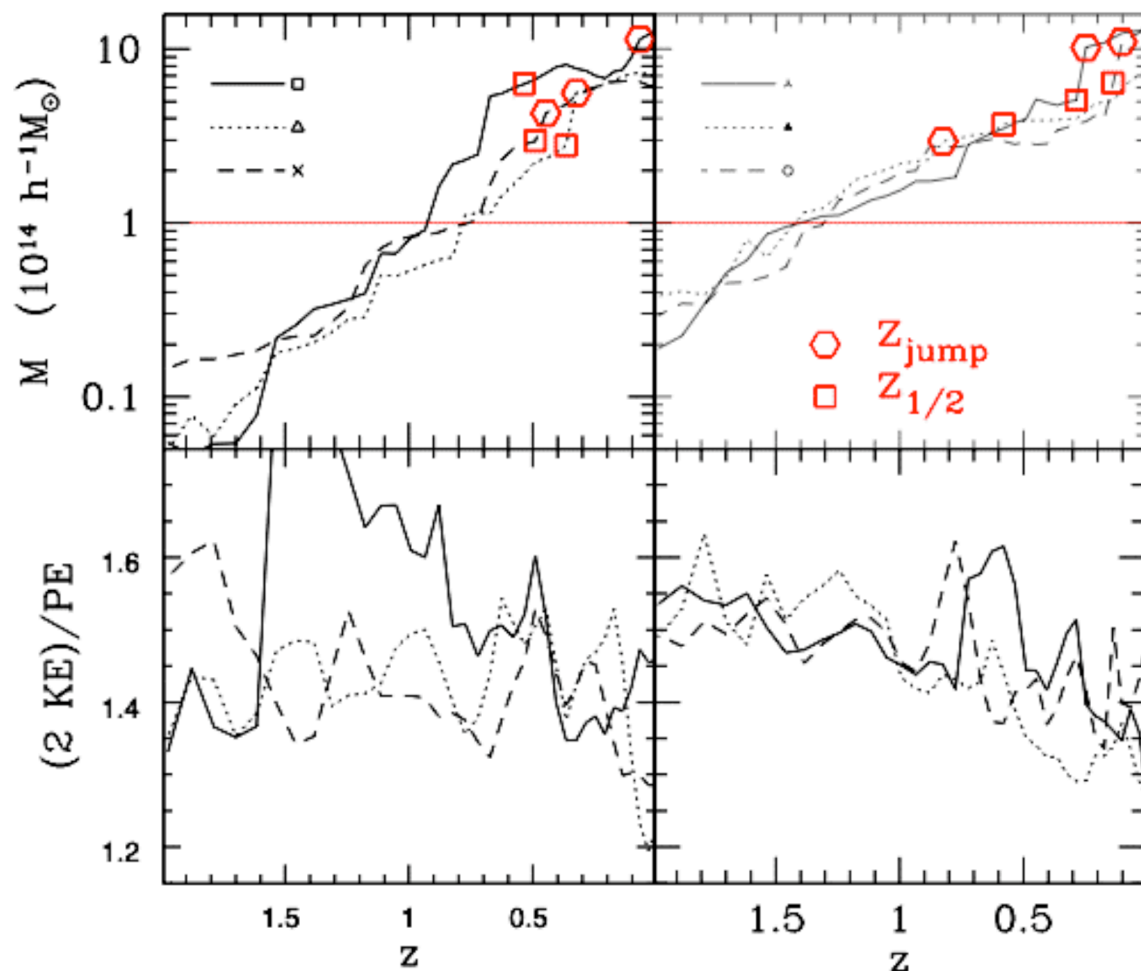
Question for students: why won't this work for spherical infall model?

## Some cluster formation times based on “events” (for $M(z)$ )

- $z_{\text{jump}}$  --time of last big mass increase in short time
  - care about this if want relaxed cluster
- $z_{1/2}$  -- time when cluster reached half its  $z=0$  mass
  - care about this if want time related to mass at ( $z=0$ )
  - see, e.g. Sheth & Tormen ‘04 (long history)
- $z_{14}$  -- time when cluster reached  $M=10^{14}h^{-1}M_{\odot}$ 
  - care about this if want deep potential well (when is halo “first” a cluster)

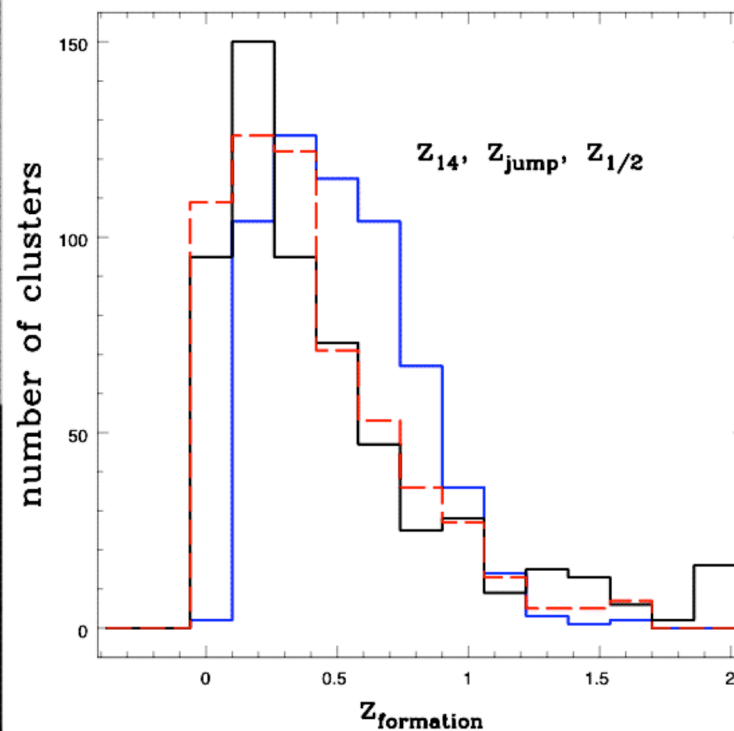
Examples....

Times for a few (6 prev) clusters:



6 clusters from before  
(note order of  $z$ 's changes)

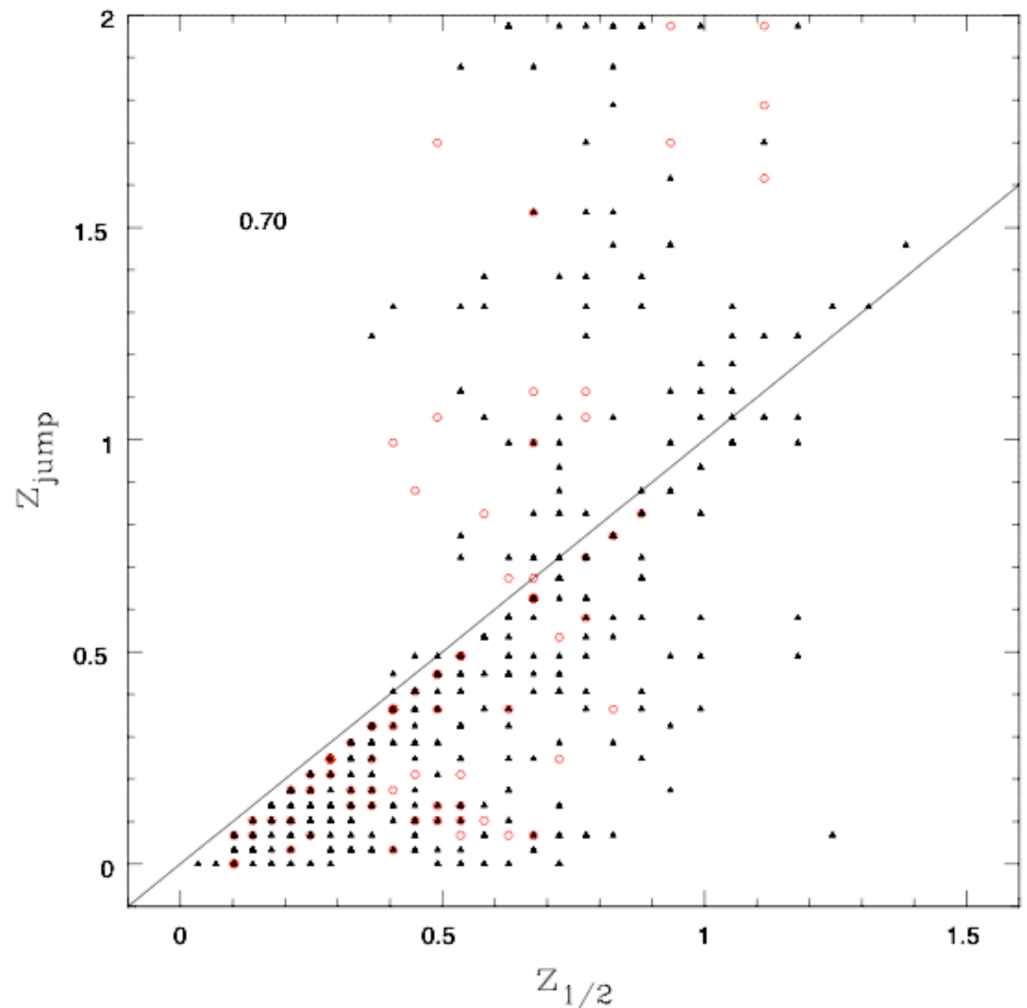
Distribution of times:



Distribution for set of  
574 clusters ( $\sigma_8 = 0.8$ )  
solid blue:  $z_{1/2}$   
solid black:  $z_{\text{jump}}$   
dashed red:  $z_{14}$

# Of course, these are related...

- Recently reaching  $z_{1/2}$   
Had jump even more recently
- Reached  $z_{1/2}$  in far past  
Most recent jump seems uncorrelated
- correlated overall
- Some clusters (13/574) never had big jumps



# Characterize this cluster formation?

- A single “formation time” (an event)
- A specific parameterization of the whole time history  $M(z)$
- Abrupt mass changes



Why would you think using the whole history would be successful?



(of largest progenitor)

- Good for galaxies

- E.g. characteristic growth curve  $M(z) = M_0 e^{-2z/(1+z_f)}$   
     $z_f$  formation time (Wechsler et al '02)
- correlated well with concentration

- Not as good for clusters: clusters are still forming!!

- Two phase models (fast and slow growth)
- add power law for two stage growth (Tasitsiomi et '04)  
     $M(z) = a^p M_0 e^{-2z/(1+z_f)}$ , solve for  $p$ ,  $z_f$
- $M(z)/M(z_{tp}) = f(\rho(z)/\rho(z_{tp}))$  (Zhao et al '03)
  - Correlated well with concentration

- How well do these different prescriptions work?

Cluster  
examples:

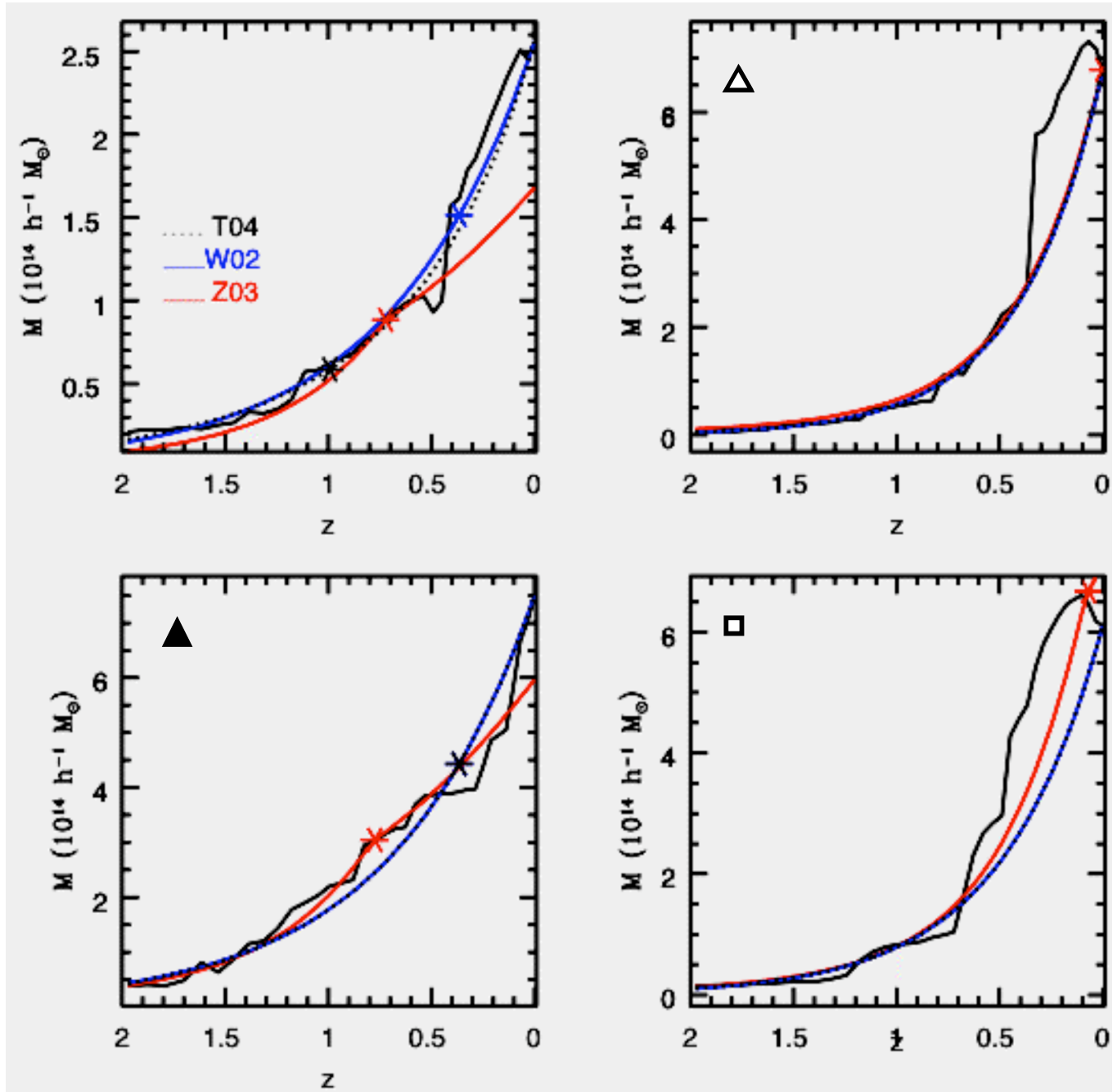
- 1 new plus 3  
from before

- sometimes

$$z_f < 0$$

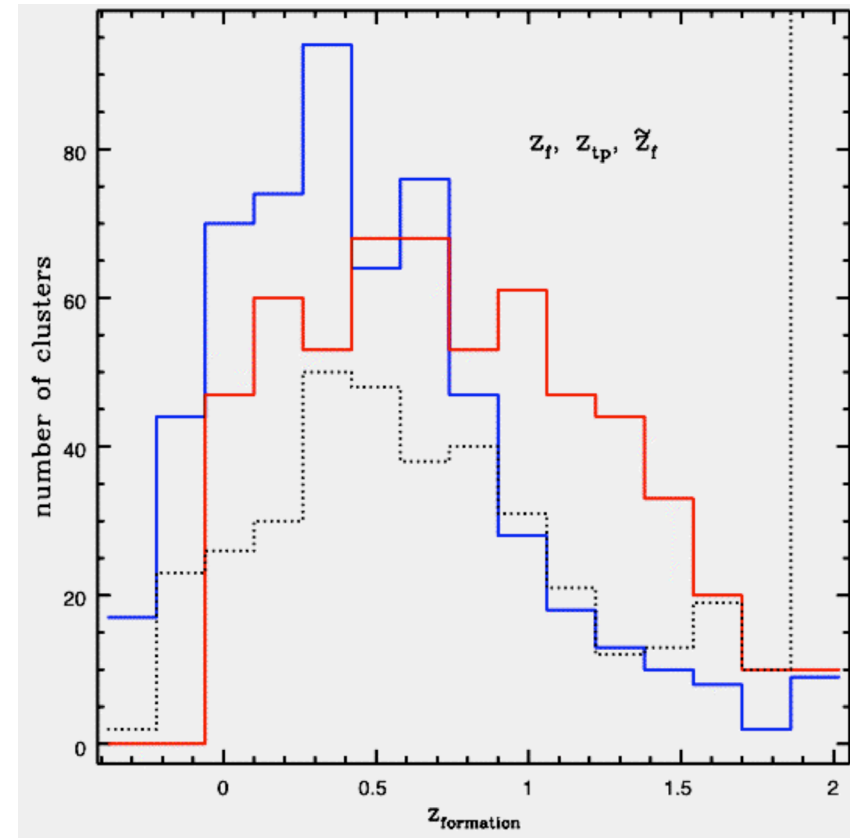
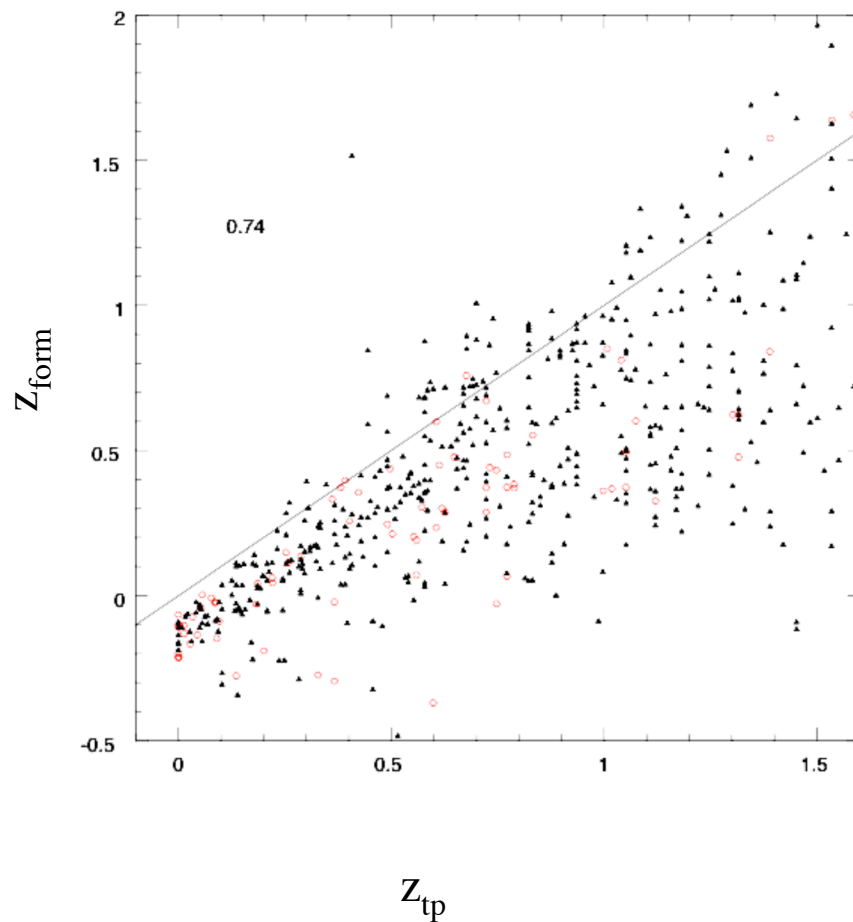
(W02,T04)

SCATTER!!



Different formation times, fits very different  
but they are correlated with each other

Scatter (Z/W) and distribution for 574 clusters (all 3)

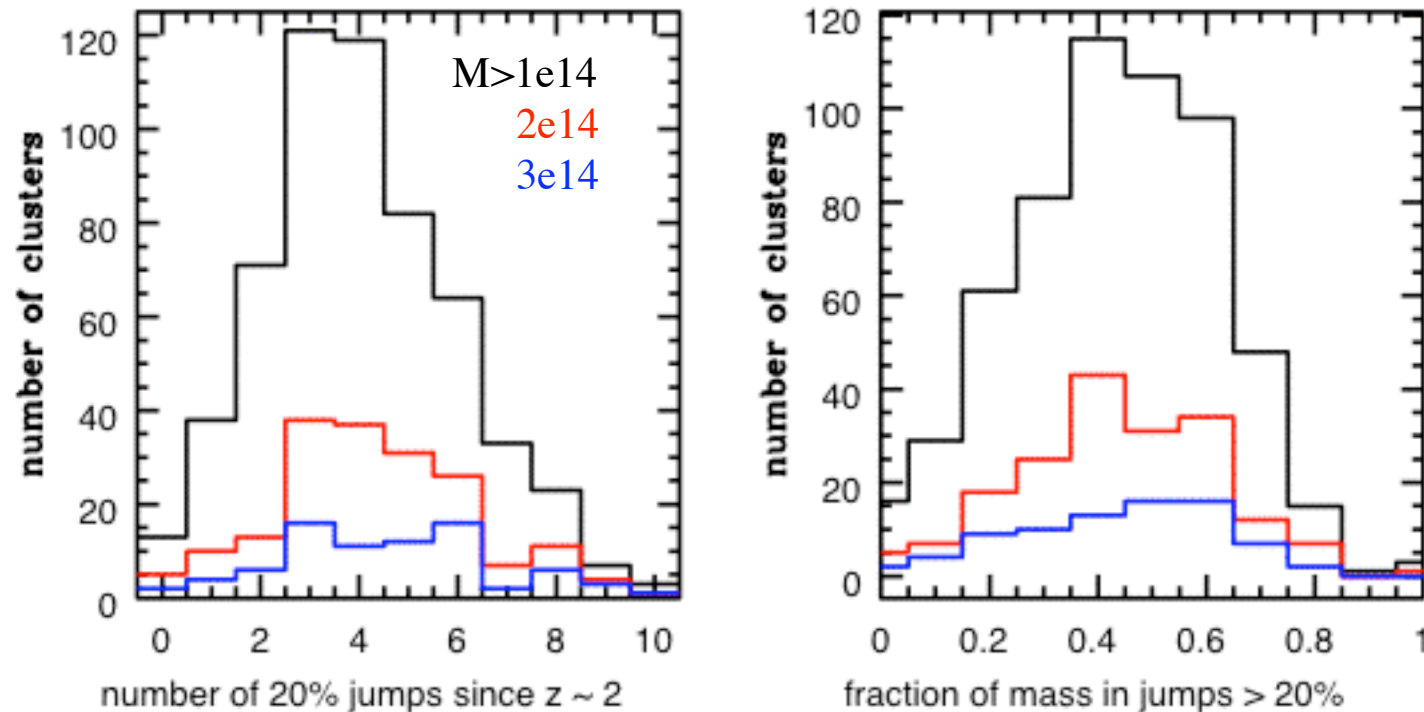


# Characterize this cluster formation?

- A single “formation time” (an event)
- A specific parameterization of the whole time history  $M(z)$
- Abrupt mass changes

# Abrupt mass changes: problem for smooth fits

- maybe these aren't a problem but a feature?
- Already used  $z_{\text{jump}}$
- Characterize clusters by number of jumps:  
At least 4 is quite common since  $z = 2$   
Lots of mass gain in these jumps



“jump”  $M_f/M_i > 1.2$  in  $\delta\tau = 100 h^{-1}\text{Mpc}$

# Mass jumps--tip of the iceberg....

If want a relaxed cluster, might want one that has had a  
**long time** since a **major merger**:

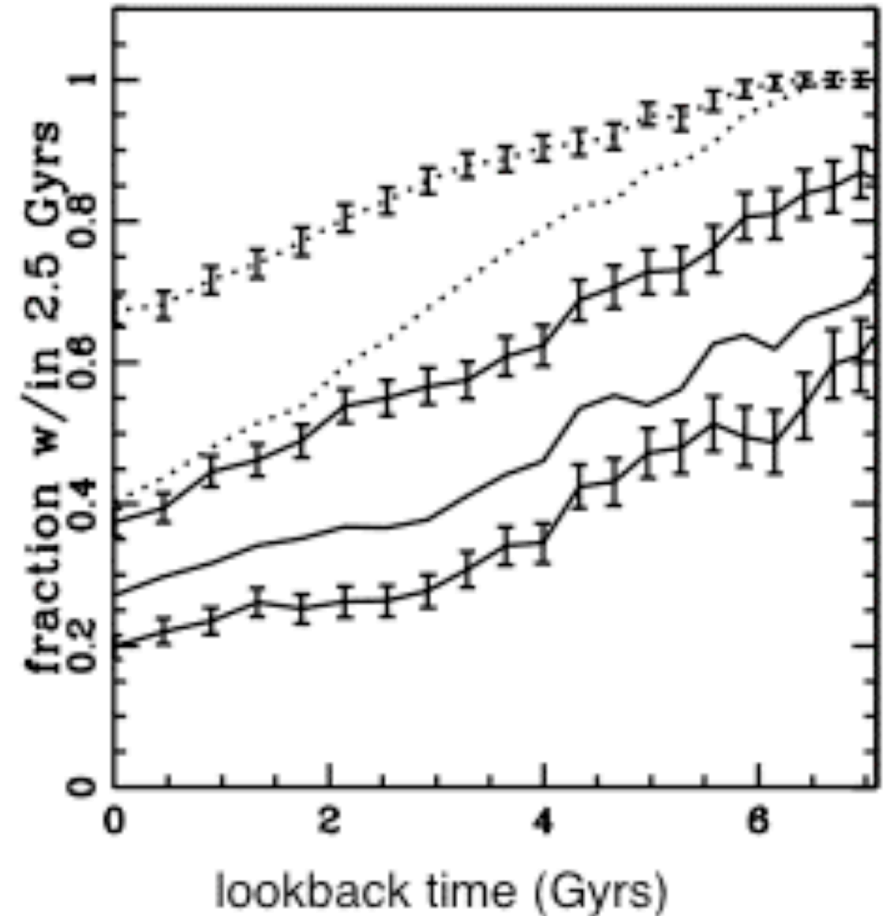
- “**long time**” --depends on what you are measuring  
(e.g. X-ray signal)
  - 2.5 Gyr, 1Gyr, 1 sound crossing?
- “**major merger**” 1:5, 1:10, 1:3,  $M_f/M_i > 1.2, 1.33$ ?
- These are all different!

Example: 2.5 Gyr relaxation time

$z \sim 0.83$  ↓

merger defn:  
(top to bottom left)

- $M_f/M_i > 1.2$
- $M_f/M_i > 1.33$
- 1:10 merger
- 1:5 merger
- 1:3 merger



Gory detail/charts/plots for different defs in our paper.

Fractions are different for different choices....but some similarities

- Fraction of clusters with recent mergers higher in past close to double for most defs between now and  $z \sim 0.83$ .
- Significant fraction are also mergers of 3 large objects
- Can combine with effects on observables (Ricker & Sarazin 2001) to get e.g.
  - survey selection functions (Randall, Sarazin, Ricker 2002)
  - an estimate of the number of relaxed clusters at a given redshift
  - an estimate of the occurrence rate of related phenomena (e.g. substructure)



## Bottom line:

Clusters are still growing, and fast!  
though not as fast as in the past  
lots of abrupt mass jumps

affects observables (...and thus mass estimates, etc.)

Relevant formation time definitions depend on what you want them for: (some correlation)

- Relaxed ( $z_{\text{jump}}$ )
- Big ( $z_{14}$ )
- Close -ish to current mass ( $z_{1/2}$ )
- Transition from fast to slow accretion ( $z_{\text{tp}}$ ) (Zhao)
- “half size” in exponential fit ( $z_f$ ) (W02,T04)

Many things you might want to know about counts for  
recently merged clusters tabulated in astro-ph/0506213

The end....